

13.1. Life-Cycle Assessment (LCA): Motivation

- ▶ The IOM reflects a *snapshot* of *all products* of a national economy in the *steady state*
- Sometimes, it is more instructive or relevant to consider the total lifetime of a single product in a time dependent way by assessing production, operation, and destruction/recycling of this product.
- This is formalized by the methods of Life-Cycle Assessment (LCA) (German: Ökobilanz).
- However, LCA only considers first-order indirect effects, e.g., CO₂ emissions caused by electric vehicles through the CO₂ footprint of electricity production
- The class of Econometric Input-Output (EIO) LCA models combines both approaches.

The standard LCA procedure

- 1. Define the life phases of the product in question:
 - production
 - operation/usage
 - destruction/recycling.
- 2. For each life phase, calculate the amount of needed materials/energy resulting in the **life-cycle inventory** \tilde{y}_j for product category j (the tilde denotes that the product is given in physical units such as kg or kWh rather than in \in).
- 3. The total emissions e_i of pollutant *i* during the life time is obtained using the emission factor matrix **C**:

$$e_i = \sum_j C_{ij} \tilde{y}_j$$

where the emission factor C_{ij} gives the units of pollutant *i* caused by one unit of product *j* (including the production chain).

Example: Gasoline vehicle

Gasoline and Diesel vehicles are two examples of internal combustion vehicles (ICV)

1. Life-cycle inventory

- ▶ $\tilde{y}_1 = 800 \text{ kg}$ steel (900 kg at production time, 80 kg spare parts during lifetime, 20 % emission-neutral recycling contribution),
- $\tilde{y}_2 = 60 \text{ kg}$ aluminum (100 kg production, 40 % of it can be recycled without additional emissions)
- $\tilde{y}_3 = 100 \,\mathrm{kg}$ plastic (40 % of which can be recycled)
- $\tilde{y}_4 = 80 \,\mathrm{kg}$ rubber (25% of which can be recycled)
- $\tilde{y}_5 = 36 \,\mathrm{kg}$ lead (three starter batteries à 12 kg)

▶ $\tilde{y}_6 = 15\,000\,\mathrm{l}$ gasoline (250 000 km at 6 l/100 km during lifetime) so we have

 $\tilde{y} = (800 \text{ kg}, 60 \text{ kg}, 60 \text{ kg}, 36 \text{ kg}, 15000 \text{ l})'.$

Example: Gasoline vehicle (ctnd)

2. Total CO₂ emissions

Defining e_1 to be the CO₂ emissions in kg (e_2 could be NO_x, e_3 PM and so on), we have

$$e_1 = \sum_{j=1}^6 C_{1j} \tilde{y}_j$$

with the row vector

$$C_{CO_2} = (C_{1j}) = (4, 30, 2, 2, 20, 2.7 \text{ kg/l}).$$

The last emission factor $C_{16} = C_{16}^{w2t} + C_{16}^{t2w}$ is the sum of two contributions:

- ▶ Well-to-tank (w2t) emissions of the production chain mining \rightarrow transport to refinery \rightarrow refining process \rightarrow transport to the gas station: $C_{16}^{w2t} = 0.4 \text{ kg/l}$,
- ► Tank-to-wheel (t2w) emissions dictated by the chemistry during the actual combustion: C^{t2w}₁₆ = 2.3 kg/l (it would be 2.7 kg/l for Diesel, i.e., the total w2w emissions of gasoline are about the t2w emissions when burning Diesel).

Example 2: Battery-electric vehicle (BEV)

- The Life-cycle inventory of steel, aluminum, rubber, plastic etc is comparable to that of the ICVs.
- The starter batteries are replaced by the Lithium driving batteries (2× 300 kg) and the gasoline is replaced by the needed electrical energy, typically 20 kWh per 100 km:

 $\tilde{y} = (800 \text{ kg}, 60 \text{ kg}, 60 \text{ kg}, 60 \text{ kg}, 600 \text{ kg}, 50000 \text{ kWh})'.$

▶ The last changed repository items lead to a new CO₂ emission factors vector

 $C_{CO_2} = (4, 30, 2, 2, 20, 0.45 \text{ kg/kWh}).$

- The Li driving batteries are expensive to produce and there is much controversy in estimating their overall emission factor C₁₅
- The energy emission factor is based, e.g., on the present (2023) German energy mix emitting 400 g CO₂ per kWh of electrical energy at the socket

Questions on LCA

- ? Is it possible to check, at a glance, whether the example BEV emits less CO₂ per km than the example ICV *when considering the driving phase alone*?
- Per 100 km, the BEV indirectly emits 20 kWh * 0.4 kg/kWh=8 kg. The ICV vehicle emits directly and indirectly 61 * 2.7 kg/l=16.2 kg. So, the BEV CO₂emissions per kilometer are about half that of the ICE (internal combustion engine, gasoline) vehicle.

However, the BEV production emissions are significantly higher. Furthermore, less than ideal efficiencies when charging/discharging have not been considered.

- **?** How would you proceed to calculate the *break-even* mileage beyond which a BEV is more environmentally friendly ("green") than the ICV?
- ! We saw that the *driving* emissions C' per kilometer x for the ICV are higher compared to the BEV. In contrast, it is the other way round for the *fixed* emissions C^0 due to production/disposal/recycling. So, just calculate the break-even kilometrage x_c by the equation

$$C^0_{\mathsf{BEV}} + C'_{\mathsf{BEV}} x_c = C^0_{\mathsf{ICV}} + C'_{\mathsf{ICVV}} x_c$$

Questions on LCA (ctnd.)

- **?** Give the two most important factors influencing the total LCA emissions of battery-electric vehicles.
 - (i) The energy mix of the used electricity (this is tricky! particularly, you cannot save your soul by paying indulgences [ger: *Ablassbriefe*] /ordering "green" electricity)
 - (ii) The production and disposal/recycling emissions of the battery and whether you need more than one battery during lifetime (to research this is even more tricky).
- A common saying states that the Sun does not issue invoices nor does the production of electric energy by photovoltaic (PV) elements entail any direct CO₂ emissions. Discuss why PV energy still has a nonzero CO₂ footprint and how to calculate the PV CO₂ emission factor. Use LCA arguments and assume a steady state.
 - (i) Get information about the usable lifetime τ ,
 - (ii) Check the climate where you want to install your PV and determine the average power (in Germany, this so-called *availability* is about 12% of the installed power P_{max}) and calculate the total electric energy delivered, e.g., $W_{\text{el}} = 0.12 \tau P_{\text{max}}$
 - (iii) Get the production and recycling emissions C of your PV including the connection to the electric grid and calculate the CO₂ footprint $e_{PV} = C/W_{el}$ [kg/kWh].

13.2. Econometric Input-Output LCA

See the German script, Chapter 5.3